

Excited states and Racah parameters of Ni²⁺ in KMgF₃ via hybrid density functional theory

Alexander Platonenko^{1,#}, Zafari Umar^{1,2}, Oleg Khyzhun^{1,3}, Mikhail G Brik^{3,5}, Michal Piasecki¹

¹ Faculty of Science and Technology, Jan Długosz University, Armii Krajowej 13/15, PL-42200, Czestochowa, Poland

² Center of Innovative Development of Science and New Technologies, National Academy of Sciences of Tajikistan, Dushanbe, 734025, Tajikistan

³ Frantsevich Institute for Problems of Materials Science, National Academy of Sciences of Ukraine, 3 Omeljan Pritsak Street, UA-03142, Kyiv, Ukraine

⁴ School of Optoelectronics & CQUPT-BUL Innovation Institute, Chongqing University of Posts and Telecommunications, Chongqing, 400065, China

⁵ Institute of Physics, University of Tartu, W. Ostwald Str. 1, 50411, Tartu, Estonia

Developing affordable materials capable of serving as host matrices for transition-metal (TM) activator ions—particularly those with unfilled 3d electron shells—has been a major scientific and engineering challenge in recent decades. These materials are essential for creating phosphors that efficiently convert excitation energy into light emission. Optical properties of the TM-dopant in the host lattice depend on charges, bond lengths, covalency, coordination and others. While the absorption energies of d-d transitions can be estimated from these parameters from ground state calculations, here we obtain these energies and electronic structures of excited state by Δ -SCF (self-consistent field) approach in solid-state physics. This approach has been used previously to predict the d-d excitation energies in bulk and surface NiO [1] in good agreement with the experimental values.

In continuation of our work on d-ions in KMgF₃[2,3], here we demonstrate results of *ab initio* calculations of 45 microstates of Ni²⁺ in a periodic KMgF₃ supercell. These include single-, double-electron and spin-flip transitions ($z^2 \uparrow \rightarrow z^2 \downarrow$), all within a single computational framework. We analyze the effect of exact exchange and correlation functionals on excitation energies, calculate Racah parameters and pressure-energy curves for every unique electron configuration. Inclusion of high amount of Hartree-Fock exact exchange is important to properly describe the ionic system and improve predicted energies of d-d transitions, CRYSTAL23 code allows to do it at very low computational cost.

This work was supported by the National Science Centre, Poland in the frame 2023/49/B/ST5/03384

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corresponding author: a.platonenko@ujd.edu.pl